

**Listing of the Claims:**

1. (Previously presented) A method of anomaly detection incorporating the steps of: -
  - a) developing a rule set of at least one anomaly characterisation rule from a training data set and any available relevant background knowledge using at least first order logic, a rule covering a proportion of positive anomaly examples of data in the training data set, and
  - b) applying the rule set to test data for anomaly detection therein.
2. (Previously presented) An automated method of anomaly detection incorporating using computer apparatus to execute the steps of: -
  - a) developing a rule set of at least one anomaly characterisation rule from a training data set and any available relevant background knowledge using at least first order logic, a rule covering a proportion of positive anomaly examples of data in the training data set, and
  - b) applying the rule set to test data for anomaly detection therein.
3. (Previously presented) A method according to Claim 2 wherein the positive anomaly examples are associated with fraud or software vulnerabilities.
4. (Previously presented) A method according to Claim 2 including developing the rule set using Higher-Order logic.
5. (Previously presented) A method according to Claim 4 including developing the rule set by:
  - a) forming an alphabet having selector functions allowing properties of the training data set to be extracted, together with at least one of the following: additional concepts, background knowledge constant values and logical AND and OR functions,
  - b) forming current rules from combinations of items in the alphabet such that type consistency and variable consistency is preserved,

- c) evaluating the current rules for adequacy of classification of the training data set,
  - d) if no current rule adequately classifies the training data set, generating new rules by applying at least one genetic operator to the current rules, a genetic operator having one of the following functions: i) combining two rules to form a new rule, ii) modifying a single rule by deleting one of its conditions or adding a new condition to it, or iii) changing one of a rule's constant values for another of an appropriate type, and
  - e) designating the new rules as the current rules and iterating steps c) onwards until a current rule adequately classifies the training data set or a predetermined number of iterations is reached.
6. (Previously presented) A method according to Claim 2 wherein data samples in the training data set have characters indicating whether or not they are associated with anomalies.
7. (Previously presented) A method according to Claim 6 for detecting telecommunications or retail fraud from anomalous data.
8. (Previously presented) A method according to Claim 7 employing inductive logic programming to develop the rule set.
9. (Previously presented) A method according to Claim 8 wherein the at least one anomaly characterisation rule has a form that an anomaly is detected or otherwise by application of the rule according to whether or not a condition set of at least one condition associated with the rule is fulfilled.
10. (Previously presented) A method according to Claim 9 wherein the at least one anomaly characterisation rule is developed by refining a most general rule by at least one of:
- a) addition of a new condition to the condition set; and
  - b) unification of different variables to become constants or structured terms.

11. (Previously presented) A method according to Claim 10 wherein a variable in the at least one anomaly characterisation rule which is defined as being in constant mode and is numerical is at least partly evaluated by providing a range of values for the variable, estimating an accuracy for each value and selecting a value having optimum accuracy.
12. (Previously presented) A method according to Claim 11 wherein the range of values is a first range with values which are relatively widely spaced, a single optimum accuracy value is obtained for the variable, and the method includes selecting a second and relatively narrowly spaced range of values in the optimum accuracy value's vicinity, estimating an accuracy for each value in the second range and selecting a value in the second range having optimum accuracy.
13. (Previously presented) A method according to Claim 12 including filtering to remove rule duplicates and rule equivalents, i.e. any rule having like but differently ordered conditions compared to another rule, and any rule which has conditions which are symmetric compared to those of another rule.
14. (Previously presented) A method according to Claim 13 including filtering to remove unnecessary 'less than or equal to' ("lteq") conditions.
15. (Previously presented) A method according to Claim 14 wherein the unnecessary lteq conditions are associated with at least one of ends of intervals, multiple lteq predicates and equality condition and lteq duplication.
16. (Previously presented) A method according to Claim 8 including implementing an encoding length restriction to avoid overfitting noisy data by rejecting a rule refinement if the refinement encoding cost in number of bits exceeds a cost of encoding positive examples covered by the refinement.
17. (Previously presented) A method according to Claim 8 including stopping construction of a rule in response to fulfilment of least one of three stopping criteria, such criteria

being:

- a) the number of conditions in any rule in a beam of rules being processed is greater than or equal to a prearranged maximum rule length,
  - b) no negative examples are covered by a most significant rule, which is a rule that:
    - i) is present in a beam currently being or having been processed,
    - ii) is significant,
    - iii) has obtained a highest likelihood ratio statistic value found so far, and
    - iv) has obtained an accuracy value greater than a most general rule accuracy value, and
  - c) no refinements were produced which were eligible to enter the beam currently being processed in a most recent refinement processing step.
18. (Previously presented) A method according to Claim 17 including adding the most significant rule to a list of derived rules and removing positive examples covered by the most significant rule from the training data set.
19. (Previously presented) A method according to Claim 8 including:
- a) selecting rules which have not met rule construction stopping criteria,
  - b) selecting a subset of refinements of the selected rules associated with accuracy estimate scores higher than those of other refinements of the selected rules, and
  - c) iterating a rule refinement, filtering and evaluation procedure to identify any refined rule usable to test data.
20. (Previously presented) Computer apparatus for anomaly detection programmed to execute the steps of:-
- a) developing a rule set of at least one anomaly characterisation rule from a training data set and any available relevant background knowledge using at least first order logic, a rule covering a proportion of positive anomaly examples of data in the training data set, and
  - b) applying the rule set to test data for anomaly detection therein.

21. (Previously presented) Computer apparatus according to Claim 20 wherein the positive anomaly examples are associated with fraud or software vulnerabilities.
22. (Previously presented) Computer apparatus according to Claim 20 programmed to develop the rule set using Higher-Order logic.
23. (Previously presented) Computer apparatus according to Claim 22 programmed to develop the rule set by:
  - a) forming an alphabet having selector functions allowing properties of the training data set to be extracted, together with at least one of the following: additional concepts, background knowledge constant values and logical AND and OR functions,
  - b) forming current rules from combinations of items in the alphabet such that type consistency and variable consistency is preserved,
  - c) evaluating the current rules for adequacy of classification of the training data set,
  - d) if no current rule adequately classifies the training data set, generating new rules by applying at least one genetic operator to the current rules, a genetic operator having one of the following functions: i) combining two rules to form a new rule, ii) modifying a single rule by deleting one of its conditions or adding a new condition to it, or iii) changing one of a rule's constant values for another of an appropriate type, and
  - e) designating the new rules as the current rules and iterating steps c) onwards until a current rule adequately classifies the training data set or a predetermined number of iterations is reached.
24. (Previously presented) Computer apparatus according to Claim 20 wherein data samples in the training data set have characters indicating whether or not they are associated with anomalies.
25. (Previously presented) Computer apparatus according to Claim 20 wherein the at least one anomaly characterisation rule has a form that an anomaly is detected or otherwise by

application of such rule according to whether or not a condition set of at least one condition associated with that rule is fulfilled.

26. (Previously presented) Computer apparatus according to Claim 20 programmed to develop the at least one anomaly characterisation rule by refining a most general rule by at least one of:
  - a) addition of a new condition to the condition set; and
  - b) unification of different variables to become constants or structured terms.
27. (Previously presented) Computer apparatus according to Claim 26 wherein a variable in the at least one anomaly characterisation rule is defined as being in constant mode and is numerical, and the computer apparatus is programmed to evaluate the at least one anomaly characterisation rule at least partly by providing a range of values for the variable, estimating an accuracy for each value and selecting a value having optimum accuracy.
28. (Previously presented) Computer apparatus according to Claim 25 programmed to filter out at least one of rule duplicates, rule equivalents and unnecessary like conditions.
29. (Previously presented) Computer apparatus according to Claim 25 programmed to stop construction of a rule in response to fulfilment of at least one of three stopping criteria, such criteria being:
  - a) the number of conditions in any rule in a beam of rules being processed is greater than or equal to a prearranged maximum rule length,
  - b) no negative examples are covered by a most significant rule, which is a rule that:
    - i) is present in a beam currently being or having been processed,
    - ii) is significant,
    - iii) has obtained a highest likelihood ratio statistic value found so far, and
    - iv) has obtained an accuracy value greater than a most general rule accuracy value, and
  - c) no refinements were produced which were eligible to enter the beam currently

being processed in a most recent refinement processing step.

30. (Previously presented) A computer software product comprising a computer readable medium containing computer readable instructions for controlling operation of computer apparatus to implement anomaly detection, wherein the computer readable instructions provide a means for controlling the computer apparatus to execute the steps of:-
  - a) developing a rule set of at least one anomaly characterisation rule from a training data set and any available relevant background knowledge using at least first order logic, a rule covering a proportion of positive anomaly examples of data in the training data set, and
  - b) applying the rule set to test data for anomaly detection therein.
31. (Previously presented) A computer software product according to Claim 30 wherein the positive anomaly examples are associated with fraud or software vulnerabilities.
32. (Previously presented) A computer software product according to Claim 30 wherein the computer readable instructions provide for controlling computer apparatus to develop the rule set using Higher-Order logic.
33. (Previously presented) A computer software product according to Claim 32 wherein the computer readable instructions provide for controlling computer apparatus to develop the rule set by:
  - a) forming an alphabet having selector functions allowing properties of the training data set to be extracted, together with at least one of the following: additional concepts, background knowledge constant values and logical AND and OR functions,
  - b) forming current rules from combinations of items in the alphabet such that type consistency and variable consistency is preserved,
  - c) evaluating the current rules for adequacy of classification of the training data set,
  - d) if no current rule adequately classifies the training data set, generating new rules by applying at least one genetic operator to the current rules, a genetic operator

- having one of the following functions: i) combining two rules to form a new rule, ii) modifying a single rule by deleting one of its conditions or adding a new condition to it, or iii) changing one of a rule's constant values for another of an appropriate type, and
- e) designating the new rules as the current rules and iterating steps c) onwards until a current rule adequately classifies the training data set or a predetermined number of iterations is reached.
34. (Previously presented) A computer software product according to Claim 30 wherein data samples in the training data set have characters indicating whether or not they are associated with anomalies.
35. (Previously presented) A computer software product according to Claim 30 wherein the at least one anomaly characterisation rule has a form that an anomaly is detected or otherwise by application of such rule according to whether or not a condition set of at least one condition associated with that rule is fulfilled.
36. (Previously presented) A computer software product according to Claim 30 wherein the computer readable instructions provide for controlling computer apparatus to develop the at least one anomaly characterisation rule by refining a most general rule by at least one of:
- a) addition of a new condition to the condition set; and
  - b) unification of different variables to become constants or structured terms.
37. (Previously presented) A computer software product according to Claim 36 wherein the computer readable instructions provide for controlling computer apparatus to at least partly evaluate a variable in the at least one anomaly characterisation rule which is defined as being in constant mode and is numerical by providing a range of values for the variable, estimating an accuracy for each value and selecting a value having optimum accuracy.

38. (Previously presented) A computer software product according to Claim 35 wherein the computer readable instructions provide for controlling computer apparatus to filter out at least one of rule duplicates, rule equivalents and unnecessary lteq conditions.
39. (Previously presented) A computer software product according to Claim 35 wherein the computer readable instructions provide for controlling computer apparatus to stop construction of a rule if in response to fulfilment of at least one of three stopping criteria, such criteria being:
  - a) the number of conditions in any rule in a beam of rules being processed is greater than or equal to a prearranged maximum rule length,
  - b) no negative examples are covered by a most significant rule, which is a rule that:
    - i) is present in a beam currently being or having been processed,
    - ii) is significant,
    - iii) has obtained a highest likelihood ratio statistic value found so far, and
    - iv) has obtained an accuracy value greater than a most general rule accuracy value, and
  - c) no refinements were produced which were eligible to enter the beam currently being processed in a most recent refinement processing step.